

$$e^{\alpha} = 1 + \frac{\alpha}{1!} + \frac{\alpha^2}{2!} + \frac{\alpha^3}{3!} + \dots + \frac{\alpha^n}{n!} + \dots = \sum_{n=0}^{\infty} \frac{\alpha^n}{n!}$$

$$: -\infty < \alpha < +\infty$$

$$\sin \alpha = \alpha - \frac{\alpha^3}{3!} + \frac{\alpha^5}{5!} - \frac{\alpha^7}{7!} + \dots + \frac{(-1)^{n-1}}{(2n-1)!} \cdot \alpha^{2n-1} + \dots = \sum_{n=1}^{\infty} \frac{(-1)^{n-1} \alpha^{2n-1}}{(2n-1)!}$$

$$: -\infty < \alpha < +\infty$$

$$\cos \alpha = 1 - \frac{\alpha^2}{2!} + \frac{\alpha^4}{4!} - \frac{\alpha^6}{6!} + \dots + \frac{(-1)^n}{(2n)!} \cdot \alpha^{2n} + \dots = \sum_{n=0}^{\infty} \frac{(-1)^n \alpha^{2n}}{(2n)!}$$

$$: -\infty < \alpha < +\infty$$

$$\ln(1 + \alpha) = \alpha - \frac{\alpha^2}{2} + \frac{\alpha^3}{3} - \frac{\alpha^4}{4} + \dots + (-1)^{n-1} \frac{\alpha^n}{n} + \dots = \sum_{n=1}^{\infty} \frac{(-1)^{n-1} \alpha^n}{n}$$

$$-1 < \alpha < 1 \quad , \quad , \quad |\alpha| < 1$$

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$$(1 + \alpha)^k = 1 + \alpha \cdot k + \frac{k(k-1)}{2!} \cdot \alpha^2 + \frac{k(k-1)(k-2)}{3!} \cdot \alpha^3 + \dots + \frac{k(k-1)(k-2) \cdot \dots \cdot (k-n+1)}{n!} \cdot \alpha^n + \dots =$$

$$= 1 + \sum_{n=1}^{\infty} \frac{k(k-1)(k-2) \cdot \dots \cdot (k-n+1)}{n!} \cdot \alpha^n$$

$$-1 < \alpha < 1 \quad (|\alpha| < 1).$$

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$$\sqrt{1 + \alpha} = 1 + \frac{1}{2}\alpha - \frac{1}{2 \cdot 4} \cdot \alpha^2 + \frac{1 \cdot 3}{2 \cdot 4 \cdot 6} \cdot \alpha^3 - \frac{1 \cdot 3 \cdot 5}{2 \cdot 4 \cdot 6 \cdot 8} \cdot \alpha^4 + \dots$$

$$\sqrt{1 - \alpha} = 1 - \frac{1}{2}\alpha - \frac{1}{2 \cdot 4} \cdot \alpha^2 - \frac{1 \cdot 3}{2 \cdot 4 \cdot 6} \cdot \alpha^3 - \frac{1 \cdot 3 \cdot 5}{2 \cdot 4 \cdot 6 \cdot 8} \cdot \alpha^4 - \dots$$

$$\frac{1}{\sqrt{1 + \alpha}} = 1 - \frac{1}{2}\alpha + \frac{1 \cdot 3}{2 \cdot 4} \cdot \alpha^2 - \frac{1 \cdot 3 \cdot 5}{2 \cdot 4 \cdot 6} \cdot \alpha^3 + \frac{1 \cdot 3 \cdot 5 \cdot 7}{2 \cdot 4 \cdot 6 \cdot 8} \cdot \alpha^4 - \dots$$

$$\frac{1}{\sqrt{1 - \alpha}} = 1 + \frac{1}{2}\alpha + \frac{1 \cdot 3}{2 \cdot 4} \cdot \alpha^2 + \frac{1 \cdot 3 \cdot 5}{2 \cdot 4 \cdot 6} \cdot \alpha^3 + \frac{1 \cdot 3 \cdot 5 \cdot 7}{2 \cdot 4 \cdot 6 \cdot 8} \cdot \alpha^4 + \dots$$

$$\frac{1}{1 + \alpha} = 1 - \alpha + \alpha^2 - \alpha^3 + \alpha^4 - \alpha^5 + \dots$$

$$\frac{1}{1 - \alpha} = 1 + \alpha + \alpha^2 + \alpha^3 + \alpha^4 + \alpha^5 + \dots$$

$$\operatorname{arctg} \alpha = \alpha - \frac{\alpha^3}{3} + \frac{\alpha^5}{5} - \frac{\alpha^7}{7} + \dots + (-1)^n \cdot \frac{\alpha^{2n+1}}{2n+1} + \dots = \sum_{n=0}^{\infty} \frac{(-1)^n \alpha^{2n+1}}{2n+1}$$

$$: -1 \leq \alpha \leq 1, \quad : |\alpha| \leq 1$$

$$\operatorname{arcsin} \alpha = \alpha + \frac{1}{2} \cdot \frac{\alpha^3}{3} + \frac{1 \cdot 3}{2 \cdot 4} \cdot \frac{\alpha^5}{5} + \frac{1 \cdot 3 \cdot 5}{2 \cdot 4 \cdot 6} \cdot \frac{\alpha^7}{7} + \dots + \frac{1 \cdot 3 \cdot 5 \cdot 7}{2 \cdot 4 \cdot 6 \cdot 8} \cdot \frac{\alpha^9}{9} + \dots + \frac{(2n-1)!! \alpha^{2n+1}}{(2n)!! (2n+1)} + \dots$$

$$: -1 \leq \alpha \leq 1, \quad : |\alpha| \leq 1$$

$$\alpha = x, \quad \alpha = -x, \alpha = 2x, \alpha = x^2, \alpha = -5x^3, \alpha = 3\sqrt{x}, \alpha = \sqrt[3]{x},$$

$$\alpha = 3x^4 \dots$$

$$\alpha = \frac{x}{2} \quad f(x) = \operatorname{arcsin} \frac{x}{2}$$

$$-1 \leq \frac{x}{2} \leq 1 \Rightarrow -2 \leq x \leq 2$$

$$1) \quad \alpha = \sqrt{x}, \quad f(x) = e^{\sqrt{x}}$$

$$: 0 \leq x < +\infty;$$

$$2) \quad \alpha = \sqrt[4]{x}, \quad f(x) = \ln(1 + \sqrt[4]{x})$$

$$0 \leq x \leq 1.$$

http://mathprofi.ru/razlozhenie_funkcij_v_stepennye_ryady.html